TRUTH

F. P. RAMSEY / PETER SULLIVAN
J. L. AUSTIN / CHARLES TRAVIS
P. F. STRAWSON / PAUL SNOWDON
MICHAEL DUMMETT / IAN RUMFITT
PETER GEACH / GRAHAM OPPY
JANE HEAL / JULIAN DODD
JENNIFER HORNSBY / GILA SHER

GUEST EDITOR
Guy Longworth, University of Warwick

© 2013 THE ARISTOTELIAN SOCIETY
In celebration of the 125th year of the Proceedings we are proud to announce our first ever Online Conference of the Aristotelian Society: a week-long event featuring a classic paper a day from our back catalogue, each accompanied by a commentary by a contemporary philosopher and an online forum open to all. The commentary will stimulate discussion by highlighting the paper’s major themes and their continuing importance to current debates; signaling challenges to specific claims and arguments; and indicating thematic connections between the various papers.

Continuing in the Society’s long tradition of publishing the proceedings of its live events, both the classic papers and commentaries will be published in our first ever Proceedings of the Aristotelian Society, The Virtual Issue, which will be free and available online following the conference.

The first Online Conference and Virtual Issue will focus on the theme of Truth. What is it for the things we say or believe to be true? Does truth depend on a relation between what we say or believe and the world? What are the natures of the things we say or believe, the bearers of truth? To what are the truth-bearers related when they are true: are they related to facts, ordinary objects, or something else? What is the required relation? We’ll want an account of the nature of truth that addresses those questions also to fit with an account of truth’s importance: why should it matter to us that what we say or believe is true rather than false? Our views about truth are liable to impact widely on our views about other things. Are moral claims or views apt to be true or false, or are they to be evaluated along different dimensions? Does truth figure in an account of the nature of belief or the nature of assertion? Is the acquisition of beliefs that are true amongst the fundamental aims of inquiry?

Each of the papers selected for the Online Conference were chosen for the distinctive answers that they advance to these questions. In some cases papers were chosen because they have had a decisive impact on later discussions, in others they were chosen because they present views and arguments that deserve more careful consideration than they have thus far received. In all cases, there is much to be gained from becoming acquainted, or reacquainted, with these important texts.

The Online Conference and Virtual Issue will be moderated and edited by Guy Longworth (Warwick).
Sir Michael Anthony Eardley Dummett, FBA, D.Litt (27 June 1925 – 27 December 2011) was, until 1992, Wykeham Professor of Logic at the University of Oxford. He wrote on the history of analytic philosophy, most notably as an interpreter of Frege, and has made original contributions to the subject, particularly in the philosophies of mathematics, logic, language and metaphysics. He was best known for his work on truth and meaning and their implications for the debates between realism and anti-realism, a term he helped popularize.

“Truth” was originally published in the Proceedings of the Aristotelian Society, Supplementary Volume LIX (1959).
FREGE held that truth and falsity are the references of sentences. Sentences cannot stand for propositions (what Frege calls 'thoughts'), since the reference of a complex expression depends only on the reference of its parts; whereas if we substitute for a singular term occurring in a sentence another singular term with the same reference but a different sense, the sense of the whole sentence, \(i.e.\) the thought which it expresses, changes. The only thing which it appears must in these circumstances remain unchanged is the truth-value of the sentence. The expressions "is true" and "is false" look like predicates applying to propositions, and one might suppose that truth and falsity were properties of propositions; but it now appears that the relation between a proposition and its truth-value is not like that between a table and its shape, but rather like that between the sense of a definite description and the actual object for which it stands.

To the objection that there are non-truth-functional occurrences of sentences as parts of complex sentences, \(e.g.,\) clauses in indirect speech, Frege replies that in such contexts we must take ordinary singular terms as standing, not for their customary reference, but for their sense, and hence we may say that in such a context, and only then, a sentence stands for the proposition it usually expresses.

If someone asks, "But what kind of entities are these truth-values supposed to be?" we may reply that there is no more difficulty in seeing what the truth-value of a sentence may be than there is in seeing what the direction of a line may be; we have been told when two sentences have the same truth-value – when they are materially equivalent – just as we know when two lines have the same direction – when they are parallel. Nor need we waste time on the objection raised by Max Black that on Frege's theory certain sentences become meaningful which we should not normally regard as such, \(e.g.,\) "If oysters are inedible, then the False". If sentences stand for truth-values, but there are also expressions standing for truth-values which are not sentences, then the objection to allowing expressions of the latter kind to stand wherever sentences can stand and \textit{vice versa} is grammatical, not logical. We often use the word "thing" to provide a noun where grammar demands one and we have only an adjective, \(e.g.,\) in "That was a disgraceful thing to do"; and we could introduce a verb, say "true", to fulfil the purely grammatical function of converting a noun standing for a truth-value into a sentence standing for the same truth-value. It may be said that
Frege has proved that a sentence does not ordinarily stand for a proposition, and has given a plausible argument that if sentences have references, they stand for truth-values, but that he has done nothing to show that sentences do have references at all. This is incorrect; Frege's demonstration that the notions of a concept (property) and a relation can be explained as special cases of the notion of a function provides a plausible argument for saying that sentences have a reference.

What is questionable is Frege's use of the words "truth" and "falsity" as names of the references of sentences; for by using these words rather than invented words of his own he gives the impression that by taking sentences to have a reference, with material equivalence as the criterion of identity, he has given an account of the notions of truth and falsity which we are accustomed to employ. Let us compare truth and falsity with the winning and losing of a board game. For a particular game we may imagine first formulating the rules by specifying the initial position and the permissible moves; the game comes to an end when there is no permissible move. We may then distinguish between two (or three) kinds of final position, which we call "Win" (meaning that the player to make the first move wins), "Lose" (similarly) and possibly "Draw". Unless we tacitly appeal to the usual meanings of the words "win", "lose" and "draw", this description leaves out one vital point – that it is the object of a player to win. It is part of the concept of winning a game that a player plays to win, and this part of the concept is not conveyed by a classification of the end positions into winning ones and losing ones. We can imagine a variant of chess in which it is the object of each player to be checkmated, and this would be an entirely different game; but the formal description we imagined would coincide with the formal description of chess. The whole theory of chess could be formulated with reference only to the formal description; but which theorems of this theory interested us would depend upon whether we wished to play chess or the variant game. Likewise, it is part of the concept of truth that we aim at making true statements; and Frege's theory of truth and falsity as the references of sentences leaves this feature of the concept of truth quite out of account. Frege indeed tried to bring it in afterwards, in his theory of assertion – but too late; for the sense of the sentence is not given in advance of our going in for the activity of asserting, since otherwise there could be people who expressed the same thoughts but went in instead for denying them.

A similar criticism applies to many accounts of truth and falsity or of the meanings of certain sentences in terms of truth and falsity. We cannot in general suppose that we give a proper account of a concept by describing those circumstances in which we do, and those in which we do not, make use of the relevant word, by describing the usage of that word; we must also give an account of the point of the concept, explain what we use the word for. Classifications do not exist in the void, but are connected always with some interest which we have, so that to assign
something to one class or another will have consequences connected
with this interest. A clear example is the problem of justifying a form of
argument, deductive or inductive. Classification of arguments into
(deductively or inductively) valid and invalid ones is not a game played
merely for its own sake, although it could be taught without reference to
any purpose or interest, say as a school exercise. Hence there is really a
problem of showing that the criteria we employ for recognising valid
arguments do in fact serve the purpose we intend them to serve: the
problem is not to be dismissed – as it has long been fashionable to do –
by saying that we use the criteria we use.

We cannot assume that a classification effected by means of a
predicate in use in a language will always have just one point. It may be
that the classification of statements into true ones, false ones, and,
perhaps, those that are neither true nor false, has one principal point,
but that other subsidiary ends are served by it which make the use of the
words "true" and "false" more complex than it would otherwise be. At
one time it was usual to say that we do not call ethical statements 'true'
or 'false', and from this many consequences for ethics were held to flow.
But the question is not whether these words are in practice applied to
ethical statements, but whether, if they were so applied, the point of
doing so would be the same as the point of applying them to statements
of other kinds, and, if not, in what ways it would be different. Again, to
be told that we say of a statement containing a singular term which lacks
reference that it is neither true nor false is so far only to be informed of a
point of usage; no philosophical consequences can yet be drawn. Rather,
we need to ask whether describing such a statement as neither true nor
false accords better with the general point of classifying statements as
true or false than to describe it as false. Suppose that we learn that in a
particular language such statements are described as 'false': how are we
to tell whether this shows that they use such statements differently from
ourselves or merely that "false" is not an exact translation of their
word? To say that we use singular statements in such a way that they are
neither true nor false when the subject has no reference is meant to
characterise our use of singular statements; hence it ought to be possible
to describe when in a language not containing words for "true" and
"false" singular statements would be used in the same way as we use
them, and when they would be used so as to be false when the subject
had no reference. Until we have an account of the general point of the
classification into true and false we do not know what interest attaches
to saying of certain statements that they are neither true nor false; and
until we have an account of how the truth-conditions of a statement
determine its meaning the description of the meaning by stating the
truth-conditions is valueless.

A popular account of the meaning of the word "true", also deriving
from Frege, is that [it is true that P] has the same sense as the sentence P.
If we then ask why it is any use to have the word "true" in the language,
the answer is that we often refer to propositions indirectly, i.e., without expressing them, as when we say "Goldbach’s conjecture" or "what the witness said ". We also generalise about propositions without referring to any particular one, e.g., in "Everything he says is true". This explanation cannot rank as a definition in the strict sense, since it permits elimination of "is true" only when it occurs attached to a "that"-clause, and not when attached to any other expression standing for a proposition or to a variable; but, since every proposition can be expressed by a sentence, this does not refute its claim to be considered as determining uniquely the sense of "is true". It might be compared with the recursive definition of "+", which enables us to eliminate the sign "+", only when it occurs in front of a numeral, and not when it occurs in front of any other expression for a number or in front of a variable; yet there is a clear mathematical sense in which it specifies uniquely what operation "+" is to signify. Similarly, our explanation of "is true" determines uniquely the sense, or at least the application, of this predicate: for any given proposition there is a sentence expressing that proposition, and that sentence states the conditions under which the proposition is true.

If, as Frege thought, there exist sentences which express propositions but are neither true nor false, then this explanation appears incorrect. Suppose that P contains a singular term which has a sense but no reference: then, according to Frege, P expresses a proposition which has no truth-value. This proposition is therefore not true, and hence the statement [It is true that P] will be false. P will therefore not have the same sense as [It is true that P], since the latter is false while the former is not. It is not possible to plead that [It is true that P] is itself neither true nor false when the singular term occurring in P lacks a reference, since the oratio obliqua clause [that P] stands for the proposition expressed by P, and it is admitted that P does have a sense and express a proposition; the singular term occurring in P has in [It is true that P] its indirect reference, namely its sense, and we assumed that it did have a sense. In general, it will always be inconsistent to maintain the truth of every instance of "It is true that p if and only if p" while allowing that there is a type of sentence which under certain conditions is neither true nor false. It would be possible to evade this objection by claiming that the "that"-clause in a sentence beginning "It is true that" is not an instance of oratio obliqua; that the word "that" here serves the purely grammatical function of transforming a sentence into a noun-clause without altering either its sense or its reference. We should then have to take phrases like "Goldbach’s conjecture" and "what the witness said" as standing not for propositions but for truth-values. The expression "is true" would then be exactly like the verb "trues" which we imagined earlier; it would simply convert a noun-phrase standing for a truth-value into a sentence without altering its sense or its reference. It might be objected that this variant of Frege’s account tallies badly with his saying that it is the thought (proposition) which is what is true or false; but we
can express this point of Frege's by saying that it is the *thought*, rather than the *sentence*, which primarily stands for a truth-value. A stronger objection to the variant account is that it leans heavily on the theory of truth-values as references of sentences, while the original version depends only on the more plausible view that clauses in indirect speech stand for propositions. In any case, if there are meaningful sentences which say nothing which is true or false, then there must be a use of the word "true" which applies to propositions; for if we say [It is neither true nor false that P], the clause [that P] must here be in *oratio obliqua*, otherwise the whole sentence would lack a truth-value.

Even if we do not wish to say of certain statements that they are neither true nor false, this account cannot give the whole meaning of the word "true". If we are to give an explanation of the word "false" parallel to our explanation of "true" we shall have to say that [It is false that P] has the same sense as the negation of P. In logical symbolism there exists a sign which, put in front of a sentence, forms the negation of that sentence; but in natural languages we do not have such a sign. We have to think to realise that the negation of "No-one is here" is not "No-one is not here" but "Someone is here"; there is no one rule for forming the negation of a given sentence. Now according to what principle do we recognise one sentence as the negation of another? It is natural to answer: The negation of a sentence P is that sentence which is true if and only if P is false and false if and only if P is true. But this explanation is ruled out if we want to use the notion of the negation of a sentence in order to explain the sense of the word "false". It would not solve the difficulty if we did have a general sign of negation analogous to the logical symbol, for the question would then be: How in general do we determine the sense of the negation, given the sense of the original sentence?

We encounter the same difficulty over the connective "or". We can give an account of the meaning of "and" by saying that we are in a position to assert [P and Q] when and only when we are in a position to assert P and in a position to assert Q. (This is not circular: one could train a dog to bark only when a bell rang *and* a light shone without presupposing that it possessed the concept of conjunction.) But, if we accept a two-valued logic, we cannot give a similar explanation of the meaning of "or". We often assert [P or Q] when we are not either in a position to assert P or in a position to assert Q. I use the word "we" here, meaning mankind, advisedly. If the history master gives the schoolboy a hint, saying, "It was either James I or Charles I who was beheaded", then the schoolboy is in a position to assert, "Either James I or Charles I was beheaded" without (perhaps) being in a position to assert either limb of the disjunction; but it is not this sort of case which causes the difficulty. The ultimate source of the schoolboy's knowledge derives from something which justifies the assertion that Charles I was beheaded; and this is all that would be required for the proposed
explanation of the word "or" to be adequate. Likewise, the explanation is not impugned by cases like that in which I remember that I was talking either to Jean or to Alice, but cannot remember which. My knowledge that I was talking either to Jean or to Alice derives ultimately from the knowledge that I had at the time that I was talking to (say) Jean; the fact that the incomplete knowledge is all that survives is beside the point. Rather, the difficulty arises because we often make statements of the form [P or Q] when the ultimate evidence for making them, in the sense indicated, is neither evidence for the truth of P nor evidence for the truth of Q. The most striking instance of this is the fact that we are prepared to assert any statement of the form [P or not P], even though we may have no evidence either for the truth of P or for the truth of [Not P].

In order to justify asserting [P or not P], we appeal to the truth-table explanation of the meaning of "or". But if the whole explanation of the meanings of "true" and "false" is given by "It is true that p if and only if p" and "It is false that p if and only if not p", this appeal fails. The truth-table tells us, e.g., that from P we may infer [P or Q] (in particular, [P or not P]); but that much we already knew from the explanation of "or" which we have rejected as insufficient. The truth-table does not show us that we are entitled to assert [P or not P] in every possible case, since this is to assume that every statement is either true or false; but, if our explanation of "true" and "false" is all the explanation that can be given, to say that every statement is either true or false is just to say that we are always justified in saying [P or not P].

We naturally think of truth-tables as giving the explanation of the sense which we attach to the sign of negation and to the connectives, an explanation which will show that we are justified in regarding certain forms of statement as logically true. It now appears that if we accept the redundancy theory of "true" and "false" – the theory that our explanation gives the whole meaning of these words – the truth-table explanation is quite unsatisfactory. More generally, we must abandon the idea which we naturally have that the notions of truth and falsity play an essential role in any account either of the meaning of statements in general or of the meaning of a particular statement. The conception pervades the thought of Frege that the general form of explanation of the sense of a statement consists in laying down the conditions under which it is true and those under which it is false (or better: saying that it is false under all other conditions); this same conception is expressed in the Tractatus in the words, "In order to be able to say that 'p' is true (or false), must have determined under what conditions I call 'p' true, and this is how I determine the sense of the sentence" (4.063). But in order that someone should gain from the explanation that P is true in such-and-such circumstances an understanding of the sense of P, he must already know what it means to say of P that it is true. If when he enquires into this he is told that the only explanation is that to say that P
is true is the same as to assert P, it will follow that in order to understand what is meant by saying that P is true, he must already know the sense of asserting P, which was precisely what was supposed to be being explained to him.

We thus have either to supplement the redundancy theory or to give up many of our preconceptions about truth and falsity. It has become a commonplace to say that there cannot be a criterion of truth. The argument is that we determine the sense of a sentence by laying down the conditions under which it is true, so that we could not first know the sense of a sentence and then apply some criterion to decide in what circumstances it was true. In the same sense there could not be a criterion for what constitutes the winning of a game, since learning what constitutes winning it is an essential part of learning what the game is. This does not mean that there may not be in any sense a theory of truth. For a particular bounded language, if it is free of ambiguity and inconsistency, it must be possible to characterise the true sentences of the language; somewhat as, for a given game, we can say which moves are winning moves. (A language is bounded if we may not introduce into it new words or new senses for old words.) Such a characterisation would be recursive, defining truth first for the simplest possible sentences, and then for sentences built out of others by the logical operations employed in the language; this is what is done for formalised languages by a truth-definition. The redundancy theory gives the general form of such a truth-definition, though in particular cases more informative definitions might be given.

Now we have seen that to say for each particular game what winning it consists in is not to give a satisfactory account of the concept of winning a game. What makes us use the same term "winning" for each of these various activities is that the point of every game is that each player tries to do what for that game constitutes winning; i.e., what constitutes winning always plays the same part in determining what playing the game consists in. Similarly, what the truth of a statement consists in always plays the same role in determining the sense of that statement, and a theory of truth must be possible in the sense of an account of what that role is. I shall not now attempt such an account; I claim, however, that such an account would justify the following. A statement, so long as it is not ambiguous or vague, divides all possible states of affairs into just two classes. For a given state of affairs, either the statement is used in such a way that a man who asserted it but envisaged that state of affairs as a possibility would be held to have spoken misleadingly, or the assertion of the statement would not be taken as expressing the speaker's exclusion of that possibility. If a state of affairs of the first kind obtains, the statement is false; if all actual states of affairs are of the second kind, it is true. It is thus prima facie senseless to say of any statement that in such-and-such a state of affairs it would be neither true nor false.
The sense of a statement is determined by knowing in what circumstances it is true and in what false. Likewise the sense of a command is determined by knowing what constitutes obedience to it and what disobedience; and the sense of a bet by knowing when the bet is won and when it is lost. Now there may be a gap between the winning of a bet and the losing of it, as with a conditional bet; can there be a similar gap between obedience and disobedience to a command, or between the truth and falsity of a statement? There is a distinction between a conditional bet and a bet on the truth of a material conditional; if the antecedent is unfulfilled, in the first case the bet is off – it is just as if no bet had been made – but in the second case the bet is won. A conditional command where the antecedent is in the power of the person given the order (e.g., a mother says to a child, "If you go out, wear your coat") is always like a bet on the material conditional; it is equivalent to the command to ensure the truth of the material conditional, *viz.*, "Do not go out without your coat". We cannot say that if the child does not go out, it is just as if no command had been given, since it may be that, unable to find his coat, he stayed in order to comply with the command.

Can a distinction parallel to that for bets be drawn for conditional commands where the antecedent is not in the person's power? I contend that the distinction which looks as if it could be drawn is in fact void of significance. There are two distinct kinds of consequence of making a bet, winning it and losing; to determine what is to involve one of these is not yet to determine completely what is to involve the other. But there is only one kind of consequence of giving a command, namely that, provided one had the right to give it in the first place, one acquires a right to punish or at least reprobate disobedience. It might be thought that punishment and reward were distinct consequences of a command in the same sense that paying money and receiving it are distinct consequences of a bet; but this does not tally with the role of commands in our society. The right to a reward is not taken to be an automatic consequence of obedience to a command, as the *right* to reproach is an automatic consequence of disobedience; if a reward is given, this is an act of grace, just as it is an act of grace if the punishment or reproach is withheld. Moreover, any action deliberately taken in order to comply with the command (to avoid disobedience to it) has the same claim to be rewarded as any other; hence to determine what constitutes disobedience to the command is thereby to determine what sort of behaviour might be rewarded, without the need for any further decision. If the child stays in because he cannot find his coat, this behaviour is as meritorious as if he goes out remembering to wear it; and if he forgets all about the order, but wears his coat for some other reason, this behaviour no more deserves commendation than if he chooses, for selfish reasons, to remain indoors. Where the antecedent is not in the person's power, it is indeed possible to regard the conditional command as analogous to the conditional bet; but since obedience to a command has no consequence...
of its own other than that of avoiding the punishment due for disobedience, there is not for such commands any significant distinction parallel to that between conditional bets and bets about a material conditional. If we regarded obedience to a command as giving a right to a reward, we could then introduce such a distinction for commands whose antecedent was in the person's power. Thus the mother might use the form, "If you go out, wear your coat", as involving that if the child went out with his coat he would be rewarded, if he went out without it he would be punished, and if he stayed indoors – even in order to comply with the command – he would be neither punished nor rewarded; while the form, "Do not go out without your coat", would involve his being rewarded if he stayed indoors.

Statements are like commands (as we use them) and not like bets; the making of a statement has, as it were, only one kind of consequence. To see this, let us imagine a language which contains conditional statements but has no counterfactual form (counterfactuals would introduce irrelevant complications). Two alternative accounts are suggested of the way in which conditionals are used in this language: one, that they are used to make statements conditionally; the other, that they represent the material conditional. On the first interpretation, a conditional statement is like a conditional bet: if the antecedent is fulfilled, then the statement is treated as if it had been an, unconditional assertion of the consequent, and is said to be true or false accordingly; if the antecedent is not fulfilled, then it is just as if no statement, true or false, had been made at all. On the second interpretation, if the antecedent is not fulfilled, then the statement is said to be true. How are we to settle which of these two accounts is the correct one? If statements are really like bets and not like commands; if there are two distinct kinds of consequence which may follow the making of a statement, those that go with calling the statement 'true' and those that go with calling it 'false', so that there may be a gap between these two kinds of consequence; then we ought to be able to find something which decides between the two accounts as definite as the financial transaction which distinguishes a bet on the truth of the material conditional from a conditional bet. It is no use asking whether these people say that the man who has made a conditional statement whose antecedent turns out false said something true or that he said nothing true or false; they may have no words corresponding to "true" and "false"; and if they do, how could we be sure that the correspondence was exact? If their using the words "true" and "false" is to have the slightest significance, there must be some difference in their behaviour which goes with their saying "true" or neither “true nor false” in this case.

It is evident on reflection that there is nothing in what they do which could distinguish between the two alternative accounts; the distinction between them is as empty as the analogous distinction for conditional commands whose antecedent is not in the person’s power. In order to fix
the sense of an utterance, we do not need to make two separate decisions – when to say that a true statement has been made and when to say that a false statement has been made; rather, any situation in which nothing obtains which is taken as a case of its being false may be regarded as a case of its being true, just as someone who behaves so as not to disobey a command may be regarded as having obeyed it. The point becomes clearer when we look at it in the following way. If it makes sense in general to suppose that a certain form of statement is so used that in certain circumstances it is true, in others false, and in yet others nothing has been said true or false, then we can imagine that a form of conditional was used in this way (von Wright actually holds that we use conditionals in this way). If P turns out true, then [If P, then Q] is said to be true or false according as Q is true or false, while if P turns out false we say that nothing was said true or false. Let us contrast this with what Frege and Strawson say about the use in our language of statements containing a singular term. If there is an object for which the singular term stands, then the statement is true or false according as the predicate does or does not apply to that object, but if there is no such object, then we have not said anything true or false. Now do these accounts tell us the sense of sentences of these two kinds? – that is, do they tell us how these statements are used, what is done by making statements of these forms? Not at all, for an essential feature of their use has not yet been laid down. Someone uttering a conditional statement of the kind described may very well have no opinion as to whether the antecedent was going to turn out true or false; that is, he is not taken as having misused the statement or misled his hearers if he envisages it as a possibility that that case will arise in which he is said not to have made a statement true or false. All that he conveys by uttering the conditional statement is that he excludes the possibility that the case will arise in which he is said to have said something false, namely that antecedent is true and consequent false. With the case of a singular statement it is quite different. Here someone is definitely either misusing the form of statement or misleading his hearers if he envisages it as a possibility that that case will arise in which what he said will be said to be neither true nor false, namely that the singular term has no reference. He conveys more by making the statement than just that he excludes the possibility of its being false; he commits himself to its being true.

Are we then to say that laying down the truth-conditions for a sentence is not sufficient to determine its sense, that something further will have to be stipulated as well? Rather than say this we should abandon the notions of truth and falsity altogether. In order to characterise the sense of expressions of our two forms, only a twofold classification of possible relevant circumstances is necessary. We need to distinguish those states of affairs such that if the speaker envisaged them as possibilities he would be held to be either misusing the statement or misleading his hearers, and those of which this is not the case: and one way of using the words "true" and "false" would be to call states of
affairs of the former kind those in which the statement was false and the others those in which the statement was true. For our conditional statements, the distinction would be between those states of affairs in which the statement was said to be false and those in which we said that it would either be true or else neither true nor false. For singular statements, the distinction would be between those states of affairs in which we said that the statement would either be false or else neither true nor false, and those in which it was true. To grasp the sense or use of these forms of statement, the twofold classification is quite sufficient; the threefold classification with which we started is entirely beside the point. Thus, on one way of using the words "true" and "false", we should, instead of distinguishing between the conditional statement's being true and its being neither true nor false, have distinguished between two different ways in which it could be true; and instead of distinguishing between the singular statement's being false and its being neither true nor false, we should have distinguished between two different ways in which it could be false.

This gives us a hint at a way of explaining the rôle played by truth and falsity in determining the sense of a statement. We have not yet seen what point there may be in distinguishing between different ways in which a statement may be true or between different ways in which it may be false, or, as we might say, between degrees of truth and falsity. The point of such distinctions does not lie in anything to do with the sense of the statement itself, but has to do with the way in which it enters into complex statements. Let us imagine that in the language of which the conditional statements we considered form part there exists a sign of negation, i.e., a word which, placed in front of a statement, forms another statement; I call it a sign of negation because in most cases it forms a statement which we should regard as being used as the contradictory of the original statement. Let us suppose, however, that when placed in front of a conditional statement [If P, then Q], it forms a statement which is used in the same way as the statement 'If P, then not Q'. Then if we describe the use of the conditionals by reference to a twofold classification only, i.e., in the same way as we describe a material conditional, we shall be unable to give a truth-functional account of the behaviour of their sign "not". That is, we should have the tables:

<table>
<thead>
<tr>
<th>P</th>
<th>Q</th>
<th>[If P, then Q]</th>
<th>[Not: if P, then Q]</th>
</tr>
</thead>
<tbody>
<tr>
<td>T</td>
<td>T</td>
<td>T</td>
<td>F</td>
</tr>
<tr>
<td>T</td>
<td>F</td>
<td>F</td>
<td>T</td>
</tr>
<tr>
<td>F</td>
<td>T</td>
<td>T</td>
<td>T</td>
</tr>
<tr>
<td>F</td>
<td>F</td>
<td>T</td>
<td>T</td>
</tr>
</tbody>
</table>

in which the truth-value of [Not: if P, then Q] is not determined by the truth-value of [If P, then Q]. If, on the other hand, we revert to our
original threefold classification, marking the case in which we said that no statement true or false had been made by "X", then we have the tables:

<table>
<thead>
<tr>
<th>P</th>
<th>Q</th>
<th>[If P, then Q]</th>
<th>[Not: if P, then Q]</th>
</tr>
</thead>
<tbody>
<tr>
<td>T</td>
<td>T</td>
<td>T</td>
<td>F</td>
</tr>
<tr>
<td>T</td>
<td>F</td>
<td>F</td>
<td>T</td>
</tr>
<tr>
<td>F</td>
<td>T</td>
<td>X</td>
<td>X</td>
</tr>
<tr>
<td>F</td>
<td>F</td>
<td>X</td>
<td>X</td>
</tr>
</tbody>
</table>

which can be quite satisfactorily accounted for by giving the table for "not":

<table>
<thead>
<tr>
<th>R</th>
<th>[Not R]</th>
</tr>
</thead>
<tbody>
<tr>
<td>T</td>
<td>F</td>
</tr>
<tr>
<td>X</td>
<td>X</td>
</tr>
<tr>
<td>F</td>
<td>T</td>
</tr>
</tbody>
</table>

(I have assumed that the statements P and Q take only the values T and F.) It now becomes quite natural to think of "T" as representing "true", "F" "false" and "X" "neither true nor false". Then we can say that their symbol "not" really is a sign of negation, since [Not P] is true when and only when P is false and false when and only when P is true. We must not forget, however, that the justification for distinguishing between the cases in which a conditional was said to have the value T and the cases in which it was said to have the value X was simply the possibility, created by this distinction, of treating "not" truth-functionally. In the same way if we have in a language an expression which normally functions as a sign of negation, but the effect of prefacing a singular statement with this expression is to produce a statement whose utterance still commits the speaker to there being an object for which the singular term stands, it is very natural to distinguish between two kinds of falsity a singular statement may have: that when the singular term has a reference, but the predicate does not apply to it, and that when the singular term lacks a reference. Let us represent the case in which the singular term has no reference by the symbol "Y", and let us suppose S to be a singular statement. Then we have the table:

<table>
<thead>
<tr>
<th>S</th>
<th>[Not S]</th>
</tr>
</thead>
<tbody>
<tr>
<td>T</td>
<td>F</td>
</tr>
<tr>
<td>Y</td>
<td>Y</td>
</tr>
<tr>
<td>F</td>
<td>T</td>
</tr>
</tbody>
</table>

Here again it is natural to think of "T" as representing "true", "F" "false" and "Y" "neither true nor false".
There is no necessity to use the words "true" and "false" as suggested above, so that we have to interpret X as a kind of truth and Y as a kind of falsity. Logicians who study many-valued logics have a term which can be employed here: they would say that T and X are 'designated' truth-values and F and Y 'undesignated' ones. (In a many-valued logic those formulae are considered valid which have a designated value for every assignment of values to their sentence-letters.) The points to observe are just these. (i) The sense of a sentence is determined wholly by knowing the case in which it has a designated value and the cases in which it has an undesignated one. (ii) Finer distinctions between different designated values or different undesignated ones, however naturally they come to us, are justified only if they are needed in order to give a truth-functional account of the formation of complex statements by means of operators. (iii) In most philosophical discussions of truth and falsity, what we really have in mind is the distinction between a designated and an undesignated value, and hence choosing the names "truth" and "falsity" for particular designated and undesignated values respectively will only obscure the issue. (iv) Saying that in certain circumstances a statement is neither true nor false does not determine whether the statement is in that case to count as having an undesignated or a designated value, i.e., whether someone who asserts the statement is or is not taken as excluding the possibility that that case obtains.

Baffled by the attempt to describe in general the relation between language and reality, we have nowadays abandoned the correspondence theory of truth, and justify our doing so on the score that it was an attempt to state a criterion of truth in the sense in which this cannot be done. Nevertheless, the correspondence theory expresses one important feature of the concept of truth which is not expressed by the law "It is true that p if and only if p" and which we have so far left quite out of account: that a statement is true only if there is something in the world in virtue of which it is true. Although we no longer accept the correspondence theory, we remain realists au fond; we retain in our thinking a fundamentally realist conception of truth. Realism consists in the belief that for any statement there must be something in virtue of which either it or its negation is true: it is only on the basis of this belief that we can justify the idea that truth and falsity play an essential role in the notion of the meaning of a statement, that the general form of an explanation of meaning is a statement of the truth-conditions.

To see the importance of this feature of the concept of truth, let us envisage a dispute over the logical validity of the statement "Either Jones was brave or he was not". A imagines Jones to be a man, now dead, who never encountered danger in his life. B retorts that it could still be true that Jones was brave, namely if it is true that if Jones had encountered danger, he would have acted bravely. A agrees with this, but still maintains that it does not need to be the case that either "Jones was brave" = "If Jones had encountered danger, he would have acted
bravely'' nor ''Jones was not brave'' If Jones had encountered danger, he would not have acted bravely'' is true. For, he argues, it might be the case that however many facts we knew of the kind which we should normally regard as grounds for asserting such counterfactual conditionals, we should still know nothing which would be a ground for asserting either. It is clear that B cannot agree that this is a possibility and yet continue to insist that all the same either ''Jones was brave'' or ''Jones was not brave'' is true; for he would then be committed to holding that a statement may be true even though there is nothing whatever such that, if we knew of it, we should count it as evidence or as a ground for the truth of the statement, and this is absurd. (It may be objected that there are assertions for which it would be out of place to ask one who made them for his evidence or grounds; but for such assertions the speaker must always either be in a position to make or in a position to deny them.) If B still wishes to maintain the necessity of ''Either Jones was brave or he was not'', he will have to hold either that there must be some fact of the sort to which we usually appeal in discussing counterfactuals which, if we knew it, would decide us in favour either of the one counterfactual or of the other; or else that there is some fact of an extraordinary kind, perhaps known only to God. In the latter case he imagines a kind of spiritual mechanism – Jones' character – which determines how he acts in each situation that arises; his acting in such-and-such a way reveals to us the state of this spiritual mechanism, which was however already in place before its observable effects were displayed in his behaviour. B would then argue thus: If Jones had encountered danger, he would either have acted bravely or have acted like a coward. Suppose he had acted bravely. This would then have shown us that he was brave; but he would already have been brave before his courage was revealed by his behaviour. That is, either his character included the quality of courage or it did not, and his character determines his behaviour. We know his character only indirectly, through its effects on his behaviour; but each character-trait must be there within him independently of whether it reveals itself to us or not.

Anyone of a sufficient degree of sophistication will reject B's belief in a spiritual mechanism; either he will be a materialist and substitute for it an equally blind belief in a physiological mechanism, or he will accept A's conclusion that ''Either Jones was brave or he was not'' is not logically necessary. His ground for rejecting B's argument is that if such a statement as ''Jones was brave'' is true, it must be true in virtue of the sort of fact we have been taught to regard as justifying us in asserting it. It cannot be true in virtue of a fact of some quite different sort of which we can have no direct knowledge, for otherwise the statement ''Jones was brave'' would not have the meaning that we have given it. In accepting A's position he makes a small retreat from realism; he abandons a realist view of character.
In order, then, to decide whether a realist account of truth can be given for statements of some particular kind, we have to ask whether for such a statement \( P \) it must be the case that if we knew sufficiently many facts of the kind we normally treat as justifying us in asserting \( P \), we should be in a position either to assert \( P \) or to assert [Not \( P \)]: if so, then it can truly be said that there must either be something in virtue of which \( P \) is true or something in virtue of which it is false. It is easy to overlook the force of the phrase "sufficiently many". Consider the statement "A city will never be built on this spot ". Even if we have an oracle which can answer every question of the kind, "Will there be a city here in 1990?" "In 2100?" etc., we might never be in a position either to declare the statement true or to declare it false. Someone may say: That is only because you are assuming the knowledge of only finitely many answers of the oracle; but if you knew the oracle's answers to all these questions, you would be able to decide the truth-value of the statement. But what would it mean to know infinitely many facts? It could mean that the oracle gave a direct answer "No" to the question, "Will a city ever be built here?": but to assume this is just like B's assumption of the existence of a hidden spiritual mechanism. It might mean that we had an argument to show the falsity of FA city will be built here in the year N irrespective of the value of N, e.g., if 'here' is the North Pole: but no-one would suggest that it must be the case that either the oracle will give an affirmative answer to some question of the form "Will there be a city here in the year .... ?" or we can find a general argument for a negative answer. Finally, it could mean that we were able to answer every question of the form, "Will there be a city here in the year .... ?": but having infinite knowledge in this sense will place us in no better position than when we had the oracle.

We thus arrive at the following position. We are entitled to say that a statement \( P \) must be either true or false, that there must be something in virtue of which either it is true or it is false, only when \( P \) is a statement of such a kind that we could in a finite time bring ourselves into a position in which we were justified either in asserting or in denying \( P \); that is, when \( P \) is an effectively decidable statement. This limitation is not trivial: there is an immense range of statements which, like "Jones was brave", are concealed conditionals, or which, like "A city will never be built here", contain – explicitly or implicitly – an unlimited generality, and which therefore fail the test.

What I have done here is to transfer to ordinary statements what the intuitionists say about mathematical statements. The sense of e.g., the existential quantifier is determined by considering what sort of fact makes an existential statement true, and this means: the sort of fact which we have been taught to regard as justifying us in asserting an existential statement. What would make the statement that there exists an odd perfect number true would be some particular number's being both odd and perfect; hence the assertion of the existential statement
must be taken as a claim to be able to assert some one of the singular statements. We are thus justified in asserting that there is a number with a certain property only if we have a method for finding a particular number with that property. Likewise, the sense of a universal statement is given by the sort of consideration we regard as justifying us in asserting it: namely we can assert that every number has a certain property if we have a general method for showing, for any arbitrary number, that it has that property. Now what if someone insists that either the statement "There is an odd perfect number" is true, or else every perfect number is even? He is justified if he knows of a procedure which will lead him in a finite time either to the determination of a particular odd perfect number or to a general proof that a number assumed to be perfect is even. But if he knows of no such procedure, then he is trying to attach to the statement "Every perfect number is even" a meaning which lies beyond that provided by the training we are given in the use of universal statements; he wants to say, as B said of "Jones was brave", that its truth may lie in a region directly accessible only to God, which human beings can never survey.

We learn the sense of the logical operators by being trained to use statements containing them, i.e., to assert such statements under certain conditions. Thus we learn to assert [P and Q] when we can assert P and can assert Q; to assert [P or Q] when we can assert P or can assert Q; to assert [For some n, F(n)] when we can assert [F(O)] or can assert [F(1)] or... We learn to assert [For every n, F(n)] when we can assert [F(O)] and [F(1)] and...; and to say that we can assert all of these means that we have a general method for establishing [F(x)] irrespective of the value of x. Here we have abandoned altogether the attempt to explain the meaning of a statement by laying down its truth-conditions. We no longer explain the sense of a statement by stipulating its truth-value in terms of the truth-values of its constituents, but by stipulating when it may be asserted in terms of the conditions under which its constituents may be asserted. The justification for this change is that this is how we in fact learn to use these statements: furthermore, the notions of truth and falsity cannot be satisfactorily explained so as to form a basis for an account of meaning once we leave the realm of effectively decidable statements. One result of this shift in our account of meaning is that, unless we are dealing only with effectively decidable statements, certain formulae which appeared in the two-valued logic to be logical laws no longer rank as such, in particular the law of excluded middle: this is rejected, not on the ground that there is a middle-truth-value, but because meaning, and hence validity, is no longer to be explained in terms of truth-values.

Intuitionists speak of mathematics in a highly anti-realist (anti-platonist) way: for them it is we who construct mathematics; it is not already there waiting for us to discover. An extreme form of such constructivism is found in Wittgenstein's Remarks on the Foundations of
**Mathematics.** This makes it appear as though the intuitionist rejection of an account of the meaning of mathematical statements in terms of truth and falsity could not be generalised for other regions of discourse, since even if there is no independent mathematical reality answering to our mathematical statements, there is an independent reality answering to statements of other kinds. On the other hand the exposition of intuitionism I have just given was not based on a rejection of the Fregean notion of a mathematical reality waiting to be discovered, but only on considerations about meaning. Now certainly someone who accepts the intuitionist standpoint in mathematics will not be inclined to adopt the platonist picture. Must he then go to the other extreme, and have the picture of our creating mathematics as we go along? To adopt this picture involves thinking with Wittgenstein that we are free in mathematics at every point; no step we take has been forced on us by a necessity external to us, but has been freely chosen. This picture is not the only alternative. If we think that mathematical results are in some sense imposed on us from without, we could have instead the picture of a mathematical reality not already in existence but as it were coming into being as we probe. Our investigations bring into existence what was not there before, but what they bring into existence is not of our own making.

Whether this picture is right or wrong for mathematics, it is available for other regions of reality as an alternative to the realist conception of the world. This shows how it is possible to hold that the intuitionist substitution of an account of the use of a statement for an account of its truth-conditions as the general form of explanation of meaning should be applied to all realms of discourse without thinking that we create the world; we can abandon realism without falling into subjective idealism. This substitution does not of course involve dropping the words "true" and "false", since for most ordinary contexts the account of these words embodied in the laws "It is true that p if and only if p" and "It is false that p if and only if not p" is quite sufficient: but it means facing the consequences of admitting that this is the whole explanation of the sense of these words, and this involves dethroning truth and falsity from their central place in philosophy and in particular in the theory of meaning. Of course the doctrine that meaning is to be explained in terms of use is the cardinal doctrine of the later Wittgenstein; but I do not think the point of this doctrine has so far been generally understood.
PRESIDENT: Sarah Broadie (St. Andrews)

PRESIDENT-ELECT: E.J. Lowe (Durham)

HONORARY DIRECTOR: Lucy O’Brien (UCL)

EDITOR: Matthew Soteriou (Warwick)

LINES OF THOUGHT SERIES EDITOR: Scott Sturgeon (Oxford)

VIRTUAL ISSUE GUEST EDITOR ON ‘TRUTH’: Guy Longworth (Warwick)

EXECUTIVE COMMITTEE: Ben Colburn (Glasgow) / Alison Hills (Oxford) / Rosanna Keefe (Sheffield) Marie McGinn (UEA) / Samir Okasha (Bristol) / Ian Rumfitt (Birkbeck) / Robert Stern (Sheffield)

EXECUTIVE ADMINISTRATOR: Mark Cortes Favis

ASSISTANT EDITOR: David Harris

EDITORIAL ASSISTANT: Lea Salje

WWW.ARISTOTELIANSOCIETY.ORG.UK